# APPLICATION OF IBEARUGBULEM'S MODEL FOR OPTIMSING SPLITTING TENSILE STRENGTH OF BASALT CONCRETE MIX 

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#### Abstract

The search for new raw materials that will compete favourably with existing ones is necessary to prevent the depletion of existing raw materials. This work investigates the suitability of basalt as coarse aggregate for the production of concrete and the application of Ibearugbulem's model for predicting the splitting tensile strength of concrete. A total of $\mathbf{2 4}$ concrete cylinders for basalt and granite samples of diameter 100 mm and length $\mathbf{2 0 0} \mathbf{m m}$ were casted and demoulded after 24 hours. The samples were cured and tested for splitting tensile strength after $\mathbf{2 8}$ days. The laboratory results were used in formulating a model which predicts the 28 days splitting tensile strength. From the analysis, it was established that the difference between the laboratory results of splitting tensile strength and predicted values of splitting tensile strength are not significant.


Keywords: Splitting tensile strength, Concrete, Basalt, Granite, Coarse aggregate, Model.

## 1. INTRODUCTION

The construction industry is faced with the challenge of sourcing for new raw materials that will prevent over reliance on the existing ones. Intensive research is required to discover raw materials that can perform in similar capacity or an improvement on the performance of existing materials.

The demand for coarse aggregates is rising from time to time as a result of increased construction as a result of township expansion and infrastructural upgrades such as hospitals, residential and public buildings, airports, schools and highways [1]. The Federal and State governments in contributing to solving housing deficits are financing several housing and real estate projects. These projects utilize high volume of coarse aggregates.

The discovery of new materials is important to technological improvement thereby solving the problem of overdependence on the conventional materials. Mix design is based on critical technical principles to achieve desired output. To predict the behavior of concrete under all loading and exposure conditions require a deep knowledge of the type, size and aggregate content which can be made possible through laboratory testing and observations [2].

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Basalt is usually dark, fine grained and columnar structure usually formed from fast cooling of magnesium - rich and iron - rich lava rising to the top [2]. Basalt rock are useful in the making of various products such as basalt reinforcement bars, basalt fabrics, continuous basalt filament wires and basalt mesh and grids. These basalt composites are applicable in soil strengthening, construction of bridges and highways, industrial floors, plastic polymer reinforcement, retrofitting and rehabilitation of engineering structures [3].

## 2. LITERATURE REVIEW

Ibearugbulem et al [4] observed that the Scheffe's model and Osadebe's model have predetermined number of experiments to be performed to enable their formulation. This is because the predetermined observation points will decide the mix ratios that can be used in the experiment. Their limitation is that they cannot be used to predict or optimize laboratory tests that are already performed. This limitation led to a search for a new regression model called Ibearugbulem's regression model which has been found to be a satisfactory option.

Ibearugbulem et al [4] assumed that the origin $\mathrm{Z}_{0}$ is zero and that since the products and quotients of constants are equal to constants, the Osadebe's model equation can be simplified as:
$F(Z)=\sum b_{m} \cdot Z_{i}^{m}$
$0 \leq m \leq \infty, 2 \leq m \leq \infty$
From equation 2.1, Ibearugbulem et al [5] deduced that:
For $m=0, b_{m}=0$
For $m=2, b_{m}=b_{i i}$ (for $Z_{i}^{2}$ term)

$$
\begin{equation*}
b_{m}=b_{i i}\left(\text { for } Z_{i}^{2} \text { term }\right) \tag{2.3}
\end{equation*}
$$

For $m=3, b_{m}=b_{i i i}$ (for $Z_{i}^{3}$ term)

$$
\begin{align*}
& b_{m}=b_{i j k}\left(\text { for } Z_{i} Z_{j} Z_{k} \text { term }\right) \\
& b_{m}=b_{i i j}\left(\text { for } Z_{i}^{2} Z_{j} \text { term }\right) \\
& b_{m}=b_{i j j}\left(\text { for } Z_{i} Z_{j}^{2} \text { term }\right) \\
& b_{m}=b_{i i k}\left(\text { for } Z_{i}^{2} Z_{k} \text { term }\right) \\
& b_{m}=b_{i k k}\left(\text { for } Z_{i} Z_{k}^{2} \text { term }\right) \\
& b_{m}=b_{i j k}\left(\text { for } Z_{j}^{2} Z_{k} \text { term }\right) \\
& b_{m}=b_{j k k}\left(\text { for } Z_{j} Z_{k}^{2} \text { term }\right) \tag{2.4}
\end{align*}
$$

For a four component mix, the equation becomes:
$\mathrm{F}(\mathrm{Z})=$
$\alpha_{1} Z_{1}+\alpha_{2} Z_{2}+\alpha_{3} Z_{2}+\alpha_{4} Z_{4}+\alpha_{12} Z_{1} Z_{2}+\alpha_{13} Z_{1} Z_{2}+\alpha_{14} Z_{1} Z_{4}+\alpha_{23} Z_{2} Z_{2}+\alpha_{24} Z_{2} Z_{4}+\alpha_{24} Z_{2} Z_{4}+\alpha_{123} Z_{1} Z_{2} Z_{2}+$ $\alpha_{124} Z_{1} Z_{2} Z_{4}+\alpha_{134} Z_{1} Z_{3} Z_{4}+\alpha_{234} Z_{2} Z_{3} Z_{4}+\alpha_{1234} Z_{1} Z_{2} Z_{3} Z_{4}$

Ibearugbulem and Ajoku [6] illustrated that the relationship between the pseudo variables $Z_{i}$ and the actual variables $S_{i}$ are expressed as:
$z_{i}=S_{i} / S$
$\mathrm{S}=\Sigma_{\mathrm{Si}}$

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Ibearugbulem et al [4] explained further that summing equation 2.6 and equation 2.7 will generate simultaneous equations presented in matrix format whose solution will produce the coefficients of Ibearugbulem's regression equation.

Equation 2.8 can be written in a simplified format as:
$[F(z) \cdot z]=[c c][a]$
Ibearugbulem et al [4] further stated that the component CC in equation 2.9 is usually a symmetric matrix usually a 7 x 7 dimension for a mixture of three component as shown in Table 1.

Table 1: Elements of CC for a three component mixture.

| E2Z1Z1 | EZZ1Z2 | EZZ1Z3 | EZZ1Z1Z2 | EZZ1Z1Z3 | EZZ1Z2Z3 | E2Z1Z1Z2Z3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2EZ1Z2 | EZZ2Z2 | E2Z2Z3 | EZZ1Z2Z2 | E2Z1Z3Z2 | E2Z2Z2Z3 | 2EZ1Z2Z3Z2 |
| E2Z1Z3 | E2Z2Z3 | 22Z3Z3 | E2Z1Z2Z3 | E2Z1Z3Z3 | E2Z2Z3Z3 | E2Z1Z2Z3Z3 |
| EEZ1Z1Z2 | EZZ1Z2Z2 | E2Z1Z2Z3 | E2Z1Z1Z2Z2 | E2Z1Z1Z2Z3 | E2Z11Z2Z2Z3 | E2Z1Z1Z2Z3Z2 |
| EZZ1Z1Z3 | EZZ1Z3Z2 | E2Z1Z3Z3 | EZZ1Z1Z2Z3 | EZZ1Z1Z3Z3 | EZZ1Z2Z3Z3 | EZZ1Z1Z2Z3Z3 |
| E2Z1Z2Z3 | E2Z1Z2Z3 | E2Z2Z3Z3 | E2Z1Z2Z2Z3 | E2Z1Z2Z3Z3 | E2Z2Z2Z3Z3 | E2Z1Z1Z2Z3Z3 |
| 22Z1Z1Z2Z3 | 2ZZ1Z2Z3Z2 | 22Z1Z2Z3Z3 | 2ZZ1Z1Z2Z3Z2 | 22Z1Z1Z2Z3Z3 | 22Z1Z11Z2Z3Z3 | 2ZZ1Z1Z2Z2Z3Z3 |

Source: Ibearugbulem et al [4].

## 3. RESEARCH METHODOLOGY

Materials constitute the various ingredients required for the production of fresh concrete such as cement, fine aggregates, coarse aggregates and water. The Ordinary Portland Cement Type-I, class 32.5 manufactured by Larfarge was used for the investigation. The Cement factory is located at Mfamosin in Akamkpa LGA of Cross River State. The cement was procured in bags from a retail outlet source in Calabar, Cross River State. Calabar River sand was used as fine aggregate throughout the investigation. The sand was prepared in accordance with the requirements of BS882: 1992 and BS 812: 1975.

The crushed granite aggregate was obtained from a quarry in Akamkpa LGA and labelled G1 and G2 while the crushed basalt was obtained from three locations in Ikom in Cross River State of Nigeria. The basalt from location 1 was labelled B1 and B2, the basalt from location 2 was labelled B3 and B4 while basalt from location 3 was labelled B5 and B6. The splitting tensile strength test was carried out in a compression testing machine. The cylindrical specimen was casted on a steel mould of diameter 100 mm and length 200 mm . Concrete samples for same compressive strength test were taken for the experiment. Three cylinders each were made from B1, B2, B3, B4, B5, B6, G1 and G2 making a total of 24 cylinders. The cylindrical samples were demoulded after 24 hours and cured in a curing tank for 28 days. The B mix was for basalt while G mix was for granite. The granite mix was used as control.

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The summary of mix design showing all the mix ratio is presented in Table 2
Table 2: Summary of mix design.

| S/N | Sample No. | Mix ratio | Cement <br> $\left(\mathbf{k g} / \mathbf{m}^{\mathbf{3}}\right)$ | Fine <br> Aggregate <br> $\left(\mathbf{k g} / \mathbf{m}^{\mathbf{3}}\right)$ | Coarse <br> Aggregate <br> $\left(\mathbf{k g} / \mathbf{m}^{\mathbf{3}}\right)$ | Water <br> $\left(\mathbf{k g} / \mathbf{m}^{\mathbf{3})}\right.$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | B1, B3, and B5 | $1: 1.96: 2.81$ | 410 | 802 | 1153 | 205 |
| 2 | B2, B4, and B6 | $1: 2.25: 2.75$ | 394.23 | 887 | 1084 | 205 |
| 3 | G1 | $1: 1.80: 2.75$ | 410 | 736 | 1127.5 | 205 |
| 4 | G2 | $1: 2.07: 2.76$ | 394.23 | 815 | 1088 | 205 |

Four ingredients were used, these are: water, cement, river sand and basalt coarse aggregates. However, the component mixtures were reduced from four to three for simplification as follows:

Water/cement ratio denoted as S1
Sand/cement ratio denoted as S2
Basalt/cement ratio denoted as S3
Similarly, Granite/cement ratio denoted as S3 for the control mix.

## 4. RESULTS OF MATHEMATICAL MODELLING OF SPLITTING TENSILE STRENGTH

The CC matrix is reduced from 14 by 14 to 7 by 7 by this transformation. The Ibearugbulem's regression model kept cement constant, thereby reducing the components from 4 to 3 . The values of $S$ are presented in Table 3 while the values of $Z$ are presented in Table 4.

Table 3: Values of $S$

| S/N | S1 | S2 | S3 | S |
| :--- | :--- | :--- | :--- | :--- |
| B1 | 0.50 | 1.96 | 2.81 | 5.27 |
| B2 | 0.52 | 2.25 | 2.75 | 5.52 |
| G1 | 0.50 | 1.80 | 2.75 | 5.05 |
| G2 | 0.52 | 2.07 | 2.76 | 5.35 |

Table 4: Values of $\mathbf{Z}$

| S/N | Z1 | Z2 | Z3 | Z1Z2 | Z1Z3 | Z2Z3 | Z1Z2Z3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| B1 | 0.0948767 | 0.3719165 | 0.5332068 | 0.0352862 | 0.0505889 | 0.1983084 | 0.0188148 |
| B2 | 0.0942029 | 0.4076087 | 0.4981884 | 0.03839792 | 0.0469308 | 0.2030659 | 0.0191294 |
| G1 | 0.0990099 | 0.3564356 | 0.5445545 | 0.03529066 | 0.0539163 | 0.1940986 | 0.0192177 |
| G2 | 0.0971963 | 0.3869159 | 0.5158879 | 0.03760678 | 0.0501424 | 0.1996052 | 0.0194009 |

The laboratory results for 28 days splitting tensile strength test of all specimen is presented in Table 5
Table 5: Splitting tensile strength test results for all specimen at $\mathbf{2 8}$ days.

| Specimen | Splitting tensile Strength $\left(\mathbf{N} / \mathrm{mm}^{2}\right)$ | Average Value | Denotation |
| :--- | :--- | :--- | :--- |
| B1 | 11.10 | 11.36 | B1 |
| B3 | 11.37 |  |  |
| B5 | 11.60 | 10.25 | B2 |
|  | 10.37 |  |  |
| B4 | 10.13 |  | G1 |
| B6 | 10.25 | - | G2 |
| G1 | 11.52 | - |  |
| G2 | 10.58 |  |  |

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Using the values of Zi for B 1 and B 2 in Table 4 and the laboratory results (R) of splitting tensile strength test in Table 5 as presented in Table 6,

Table 6: Matrix $\mathbf{Z}$ and $\mathbf{R}$

| Z1 | Z2 | Z3 | Z1Z2 | Z1Z3 | Z2Z3 | Z1Z2Z3 | R= |
| :--- | :--- | :--- | :--- | :--- | :---: | :---: | :--- | :--- |
| 0.0948767 | 0.3719165 | 0.533207 | 0.03529 | 0.05059 | 0.19831 | 0.018815 | 11.36 |
| 0.0942029 | 0.4076087 | 0.498188 | 0.0384 | 0.04693 | 0.20307 | 0.019129 | 10.25 |

ZR is a product of matrix Z and R and summation is found as shown in Table 7
Table 7: Summation of ZR

| $Z 1 F(Z)$ | $Z 2 F(Z)$ | Z3 F(Z) | Z1Z2 <br> $F(Z)$ | Z1Z3 <br> $F(Z)$ | Z2Z3 <br> $F(Z)$ | $Z 1 Z 2 Z 3$ <br> $F(Z)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1.077799 | 4.224971 | 6.057229 | 0.400849 | 0.574691 | 2.252779 | 0.213736 |
| 0.96558 | 4.177989 | 5.106431 | 0.39358 | 0.481043 | 2.081427 | 0.196076 |
| $\mathbf{2 . 0 4 3 3 7 9}$ | $\mathbf{8 . 4 0 2 9 6 1}$ | $\mathbf{1 1 . 1 6 3 6 6}$ | $\mathbf{0 . 7 9 4 4 2 8}$ | $\mathbf{1 . 0 5 5 7 3 4}$ | $\mathbf{4 . 3 3 4 2 0 5}$ | $\mathbf{0 . 4 0 9 8 1 2}$ |

Substituting [ $\mathrm{F}(\mathrm{Z}), \mathrm{Z}$ ] and the inverse CC matrix into the equation 2.9, the coefficient $[\alpha]$ is obtained as shown in Table 8
$[F(Z), Z]=[C C][a]$
$[a]=[F(Z) \cdot Z][C C]^{-1}$
The multiplication process is shown in Tables 8, 9 and 10
Table 8: Matrix $[C C]^{-1}$

| $[C C]^{-1}$ |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -11807736.42 | -602729.339 | -554655.777 | -5892962.18 | -7756856.2 | 60.9933272 | 38.8199987 |
| -602730.5221 | -258307.715 | 159745.8435 | 3414004.305 | -1035685.9 | 3.82344896 | 44.4319351 |
| -554655.9986 | 159746.182 | -180523.493 | -1046545.52 | 2498464.54 | 7.66318872 | 19.4307277 |
| -5892959.32 | 3414008.791 | -1046543.86 | -30586934.9 | 18314987.9 | 70.892079 | 39.9208415 |
| -7756859.207 | -1035687.9 | 2498463.323 | 18314981.35 | -16944527 | 20.5619537 | 47.6953936 |
| -57.92732572 | 2.047186947 | 8.207684133 | 86.80594908 | 11.0329569 | 0.00024624 | -173.42787 |
| -38.81997619 | 44.43194016 | 19.43072223 | 39.92074406 | 47.6954434 | 173.427845 | 0.00100978 |

Table 9: Matrix F(Z).Z

| $\mathrm{F}(\mathrm{Z}) . \mathrm{Z}$ |
| :--- |
| 2.043379 |
| 8.402961 |
| 11.16366 |
| 0.794428 |
| 1.055734 |
| 4.334205 |
| 0.409812 |

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Table 10: Matrix $[F(Z) \cdot Z][C C]^{-1}$

| 21.56666 | 21.56666 | 21.56666 | 21.56666 | 21.56666 | 21.56666 | 21.56666 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -1.689 | -1.689 | -1.689 | -1.689 | -1.689 | -1.689 | -1.689 |
| 15.6947 | 15.6947 | 15.6947 | 15.6947 | 15.6947 | 15.6947 | 15.6947 |
| -64.8883 | -64.8883 | -64.8883 | -64.8883 | -64.8883 | -64.8883 | -64.8883 |
| 76.221 | 76.221 | 76.221 | 76.221 | 76.221 | 76.221 | 76.221 |
| $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ | $-6.5 \mathrm{E}-05$ |
| -0.0018 | -0.0018 | -0.0018 | -0.0018 | -0.0018 | -0.0018 | -0.0018 |

Table 11: Values of coefficient $[\alpha]$

| $\alpha 1$ | $\alpha 2$ | $\alpha 3$ | $\alpha 12$ | $\alpha 13$ | $\alpha 23$ | $\alpha 123$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 21.5667 | -1.6890 | 15.6947 | -64.8883 | 76.2210 | -0.000065 | -0.0018 |

From the three component equation,
$\mathrm{F}(\mathrm{Z})=\alpha_{1} Z 1+\alpha_{2} Z 2+\alpha_{3} Z 3+\alpha_{12} Z 1 Z 2+\alpha_{13} Z 1 Z 3+\alpha_{23} Z 2 Z 3+\alpha_{123} Z 1 Z 2 Z 3$

Therefore, substituting the values of [ $\alpha]$ in Table 11 into equation 4.2, the optimization equation for predicting the 28 day splitting tensile strength of basalt concrete is:

## $\mathrm{F}(\mathrm{Z})=21.5667 Z 1-1.689 Z 2+15.695 Z 3-64.883 Z 1 Z 2+76.221 Z 1 Z 3-0.000065 Z 2 Z 3-$ 0.0018Z1Z2Z3

The model in equation 4.3 is used in predicting the 28 days splitting tensile strength and the predicted values alongside the laboratory values are presented in Table 13 and the predicted values for the control mix is presented in table 14 as computed in Table 12

Table 12: Computation of predicted model values of splitting tensile strength of beams.

| Model | B1 | B2 | G1 | G2 |
| :--- | :--- | :--- | :--- | :--- |
| 21.5667 Z 1 | 2.046177326 | 2.031645683 | 2.13531681 | 2.096203443 |
| -1.689 Z 2 | -0.628166969 | -0.688451094 | -0.602019728 | -0.653500955 |
| $15.6947 \mathrm{Z3}$ | 8.368520764 | 7.818917481 | 8.546619511 | 8.096705824 |
| -64.8883 Z 1 Z 2 | -2.289648554 | -2.491580943 | -2.289950933 | -2.440240023 |
| $76.221 \mathrm{Z} 1 \mathrm{Z3} 3$ | 3.855944169 | 3.577127751 | 4.109554302 | 3.82190387 |
| -0.000065 Z 2 Z 3 | $-1.289 \mathrm{E}-05$ | $-1.31993 \mathrm{E}-05$ | $-1.26164 \mathrm{E}-05$ | $-1.29743 \mathrm{E}-05$ |
| $-0.0018 \mathrm{Z} 1 \mathrm{Z} 2 \mathrm{Z3}$ | $-3.38666 \mathrm{E}-05$ | $-3.44329 \mathrm{E}-05$ | $-3.45919 \mathrm{E}-05$ | $-3.49216 \mathrm{E}-05$ |
| $\mathbf{\Sigma}$ | $\mathbf{1 1 . 3 5 2 7 7 9 9 8}$ | $\mathbf{1 0 . 2 4 7 6 1 1 2 5}$ | $\mathbf{1 1 . 8 9 9 4 7 2 7 5}$ | $\mathbf{1 0 . 9 2 1 0 2 4 2 6}$ |

Table 13: Values of predicted 28 days splitting tensile strength with laboratory values.

| $\mathbf{S} / \mathbf{N}$ | $\mathbf{B 1}$ | B2 |
| :--- | :--- | :--- |
| $C_{\text {Lab }}\left(\mathrm{N} / \mathrm{mm}^{2}\right)$ | 11.360 | 10.250 |
| $C_{\text {Model }}\left(\mathrm{N} / \mathrm{mm}^{2}\right)$ | 11.353 | 10.248 |

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Table 14: Values of predicted 28 days splitting tensile strength of control mix with laboratory values.

| $\mathbf{S} / \mathbf{N}$ | G1 | G2 |
| :--- | :--- | :--- |
| $C_{\text {Lab }}\left(\mathrm{N} / \mathrm{mm}^{2}\right)$ | 11.520 | 10.580 |
| $C_{\text {Model }}\left(\mathrm{N} / \mathrm{mm}^{2}\right)$ | 11.899 | 10.921 |

The Fisher $F$ test was carried out on the control mix to ascertain whether there is significant difference between the values of splitting tensile strength of concrete obtained from the laboratory and the values obtained from the model. The results of the F test is presented in Table 15

Table 15: Fisher $F$ test on splitting tensile strength from model using control mix.

| Response <br> Symbol | $\boldsymbol{C}_{\text {Lab }}$ | $\boldsymbol{C}_{\text {ModeI }}$ | $\left(\boldsymbol{C}_{\text {Lab }}-\boldsymbol{M}\right)$ | $\left(\boldsymbol{C}_{\text {ModeI }}-\boldsymbol{Q}\right)$ | $\left(\boldsymbol{C}_{\text {Lab }}-\boldsymbol{M}\right)^{2}$ | $\left(\boldsymbol{C}_{\text {Model }}-\boldsymbol{Q}\right)^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| G1 | 11.520 | 11.899 | 0.47 | 0.489 | 0.2209 | 0.239121 |
| G2 | 10.580 | 10.921 | -0.47 | -0.489 | 0.2209 | 0.239121 |
| Total | 22.10 | 22.820 | - | - | 0.4418 | 0.478242 |
| Mean | 11.05 | 11.41 | - | - | - | - |

Legend:
$C_{L a b}=$ Laboratory values of splitting tensile strength
$C_{\text {Model }}=$ Splitting tensile strength predicted by model
$M=$ Mean of laboratory values of splitting tensile strength
$Q=$ Mean of splitting tensile strength predicted by model
$N=$ Number of observations $=2$
Hence,
$S_{L}^{2}=\Sigma\left(C_{L a b}-M\right)^{2} / N-1$
$S_{M}^{2}=\Sigma\left(C_{\text {Model }}-Q\right)^{2} / N-1$
$S_{L}^{2}=\frac{0.4418}{2-1}=0.4418$
$S_{M}^{2}=\frac{0.478242}{2-1}=0.478242$
Since the greater value is taken as $S_{1}^{2}$. Hence,
$S_{1}^{2}=0.478242$
$S_{2}^{2}=0.4418$
$f_{\text {calculated }}=\frac{s_{1}^{2}}{s_{2}^{2}}=\frac{0.479242}{0.4418}=10.825$
Hence, $\frac{1}{f}=0.0924$
From statistical tables,
$f_{0.05}(1,1)=161.45$

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Therefore, the condition $\frac{1}{f}<\quad \frac{s_{1}^{2}}{s_{2}^{2}}<f$ is satisfied, hence, the difference between the laboratory values of splitting tensile strength and the predicted values from the model is not significant as the calculated value of F is less than the table value of F .

The student T test was carried out on the control mix to ascertain whether there is significant difference between the values of splitting strength of concrete obtained from the laboratory and the values obtained from the model. The results of the T test is presented in Table 16

Table 16: Student $T$ test on splitting tensile strength.

| Response <br> Symbol | $\boldsymbol{C}_{\boldsymbol{L}}$ | $\boldsymbol{C}_{\boldsymbol{M}}$ | $\left(\boldsymbol{C}_{\boldsymbol{M}}-\boldsymbol{C}_{\boldsymbol{L}}\right)=\boldsymbol{X}$ | $\boldsymbol{D}-\boldsymbol{X}$ | $(\boldsymbol{D}-\boldsymbol{X})^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| B1 | 11.36 | 11.353 | -0.007 | 0.1848 | 0.03415104 |
| B2 | 10.25 | 10.248 | -0.002 | 0.1798 | 0.03232804 |
| G1 | 11.52 | 11.899 | 0.379 | -0.2012 | 0.04048144 |
| G2 | 10.58 | 10.921 | 0.341 | -0.1632 | 0.02663424 |
| Total | - | - | $\mathbf{0 . 7 1 1}$ | - | $\mathbf{0 . 1 3 3 5 9 4 7 6}$ |

Legend:
$C_{L}=$ Laboratory values of splitting tensile strength
$C_{M}=$ Splitting tensile strength predicted by model
$N=$ Number of observations $=4$
Hence,
$\mathrm{D}=\Sigma \frac{\left(C_{M}-C_{D}\right)}{N}=\frac{0.711}{4}=0.1778$
$S^{2}=\Sigma \frac{(D-X)^{2}}{N-1}$
$S^{2}=\frac{0.13259476}{4-1}=0.04453$
$S=\sqrt{0.04453}$
$S=0.211$
$t=D \frac{\sqrt{N}}{s}$
$t=0.1778 \frac{\sqrt{4}}{0.211}=1.6853$
$t$ Value from the table is given as $t_{\alpha_{d} / N_{\mu}[V]}$ where $V=N-1$
Therefore $t_{0.05 / 4 /(3)}=t_{0.0125 \text { (3) }}$
From statistical table, $t_{0.0125(3)}=5.516$ by interpolation

## 5. DISCUSSION

The model equation developed is used in predicting the 28 day splitting tensile strength of concrete mix. The Fisher F test was carried out on the control mix to ascertain whether there is significant difference between the values of splitting tensile strength of concrete obtained from the laboratory and the values obtained from the model. The T test was also carried out on the to ascertain whether there is significant difference between the values of splitting tensile strength of concrete obtained from the laboratory and the values obtained from the model. The analysis show clearly that the

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difference between the predicted values and the laboratory values of splitting tensile strength are not significant. With the model developed, developers do not need to go to the laboratory to carry out rigorous test to obtain results of splitting tensile strength.

## 6. CONCLUSIONS

From the statistical analysis of Fisher F-test, the condition $\frac{1}{f}<\frac{s_{1}^{2}}{s_{2}^{2}}<f$ is satisfied, hence, the difference between the laboratory values of splitting tensile strength and the predicted values from the model is not significant as the calculated value of $F$ is less than the table value of $F$.

Similarly, from the student T-test, since $t$ from the statistical table is greater than the value of calculated $t$, the difference between the laboratory values of splitting tensile strength and the predicted values from the model is not significant.

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## REFERENCES

[1] Engidasew T A and Barbieri G. Geo-engineering evaluation of Termaber basalt rock mass for crushed stone aggregate and building stone from Central Ethiopia. Journal of African earth sciences. Vol. 99, 2013, Pp. 581-594.
[2] Kishore S, Mounika L, Pasad C M and Krisha B H. Experimental study on the use of basalt aggregates in concrete mixes. SSRG international journal of civil engineering. Vol. 2, issue 4, 2015, Pp. 39-42.
[3] Sunny J. E, Varghese R. A, Sagar S, John S. P and Kassim R. Application of basalt and its products in civil engineering. International journal of engineering research. Vol. 9, issue 6, 2020, Pp. 511-515.
[4] Ibearugbulem O M, Ettu L O, Ezeh J C and Anya U C. A new regression model for optimising concrete mixes. International journal of engineering sciences and research. Vol. 2, issue 7, 2013, Pp. 1735-1742.
[5] Ibearugbulem O M, Amanambu I K and Elogu T I. Application of Ibearugbulem's model for optimising granite concrete mix. International journal of research engineering and technology. Vol. 3, issue 3, 2014, Pp. 405-408.
[6] Ibearugbulem O M and Ajoku C A (2016). Prediction of the flexural strength of light weight periwinkle shell-river gravel concrete. International journal of engineering sciences and research technology. Vol. 5, issue 2, 2016, Pp.732-744.

